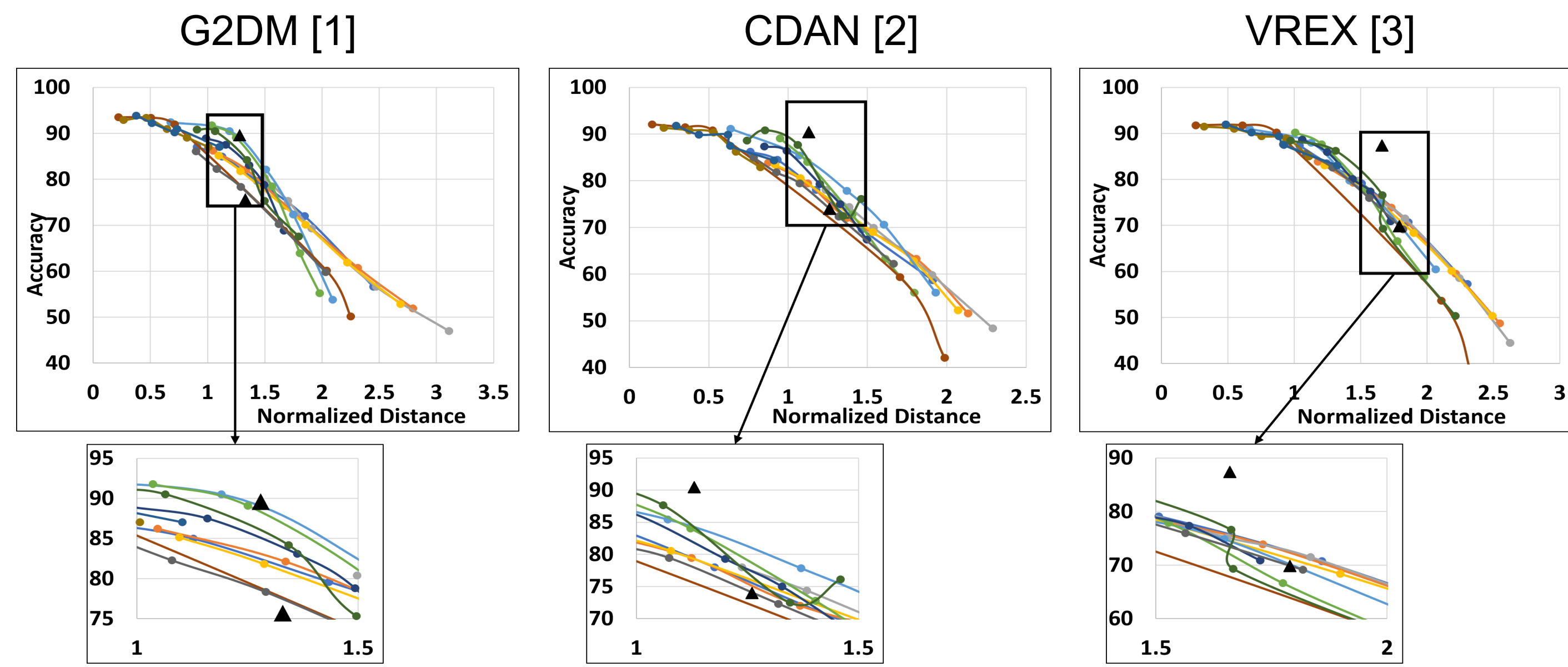


## Motivation

- Domain Generalization (DG) focuses on developing models that generalize well to data from domains unseen during training.
- Following works that explain the generalization performance using distributional distance, learning a representation space that reduces distance between domains is shown to be effective at DG.
- However, evaluating DG models only using benchmark datasets is insufficient to gauge their performance on unseen domains.



## Contributions

- We propose a data independent and a distance-based evaluation method for DG based on distributionally robust optimization.
- Our method *efficiently* estimates the loss of the worst-case distribution to better gauge the generalization performance of DG models. It can be easily incorporated into training of DG models to produce models that generalize better on unseen domains.

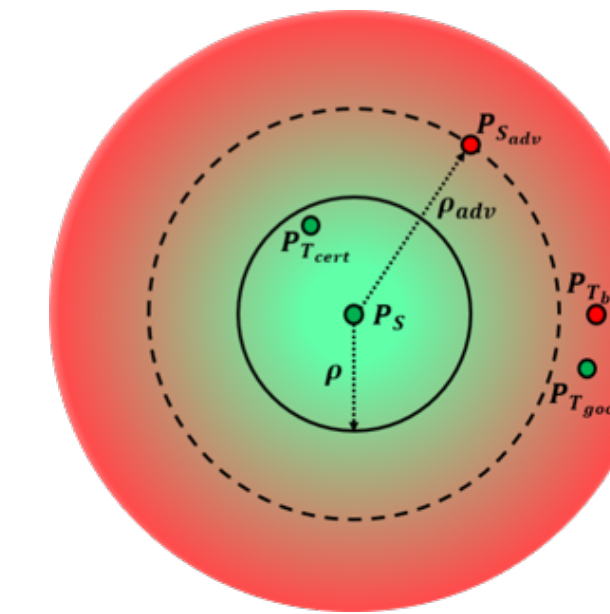
## Distance-based evaluation method for DG

- Notation:  $\mathcal{X}$ ,  $\mathcal{Y}$  denotes the data domain and the labels,  $g: \mathcal{X} \rightarrow \mathcal{Z}$  denotes the representation map and  $h: \mathcal{Z} \rightarrow \mathcal{Y}$  denotes the classifier on top of  $\mathcal{Z}$ .
- Our distance-based measure of the performance of DG model relies on the worst-case loss of the model at a particular distance  $\sup_{\mathcal{P}: \mathcal{W}_2(\mathcal{P}, \mathcal{Q}) \leq \rho} \mathbb{E}_{(x,y) \sim \mathcal{P}} [\ell(h(g(x)), y)]$ . This is an infinite-dimensional problem over a convex set and is difficult to solve.
- However, its optimal value can be computed using the dual problem. Moreover, since DG methods learn a representation space where unseen domains lie close to the source domain, we solve the following to compute the worst-case loss

$$\sup_{\mathcal{P}: \mathcal{W}_2(\mathcal{P}, g\#Q) \leq \rho} \mathbb{E}_{(z,y) \sim \mathcal{P}} [\ell(h(z), y)]$$

$$= \inf_{\gamma \geq 0} \left\{ \gamma \rho^2 + \mathbb{E}_{(z_0, y_0) \sim g\#Q} \left[ \sup_{z \in \mathcal{Z}} \{ \ell(h(z), y) - \gamma \|z_0 - z\|_2^2 \} \right] \right\}.$$

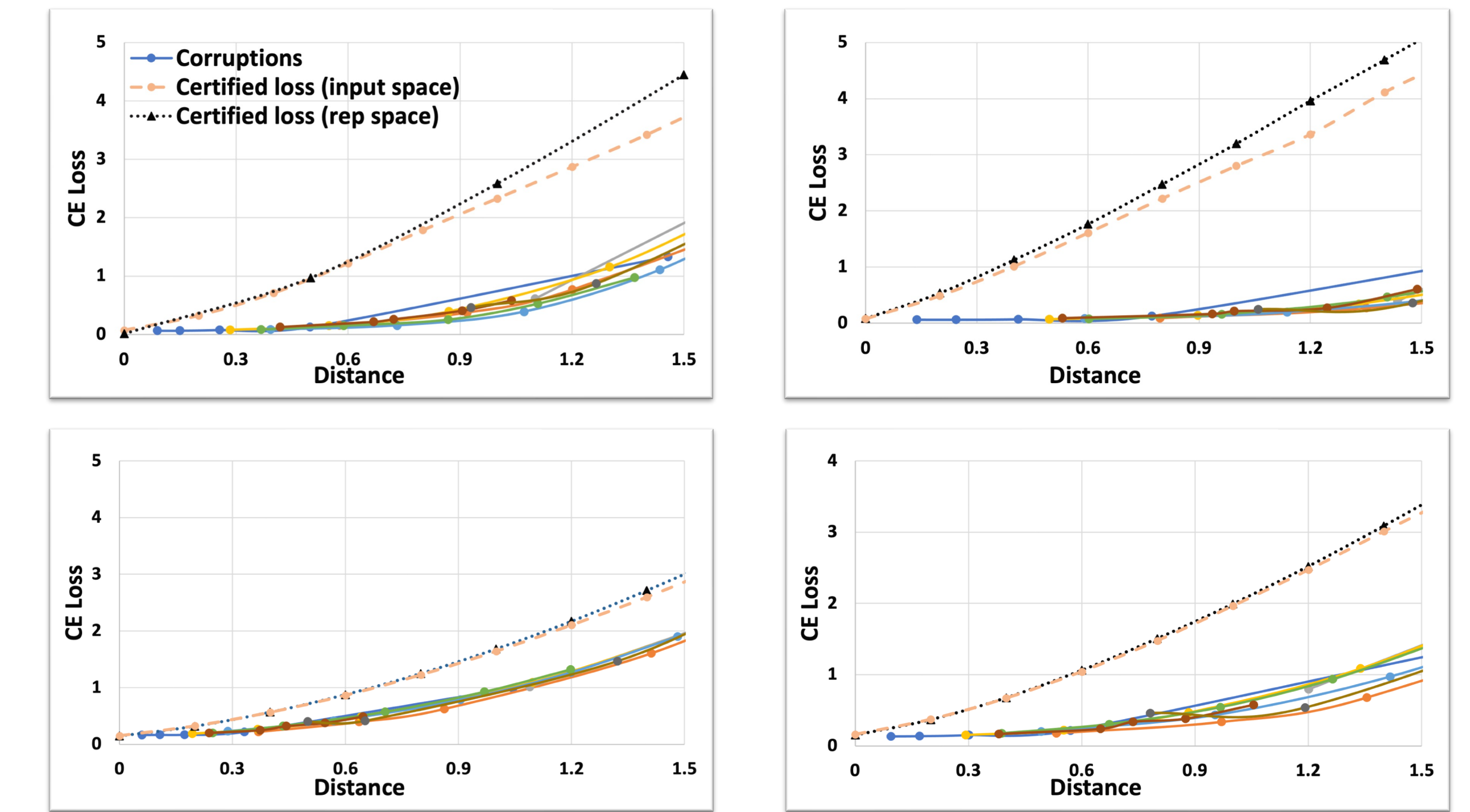
- The space of probability distributions with Wasserstein distance as a metric.  $\mathcal{P}_S$  and  $\mathcal{P}_T$  are the sources and the unseen target distributions. The worst-case loss can be efficiently computed for any distance  $\rho$  by solving the above problem.



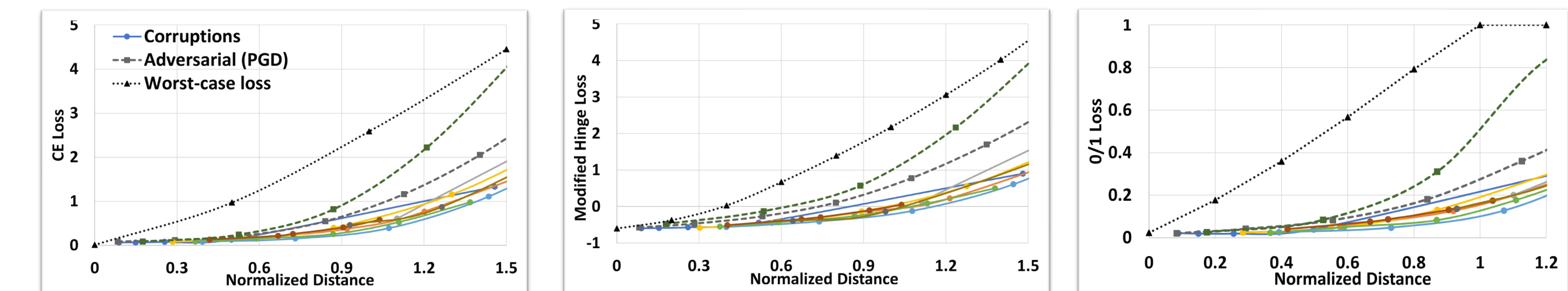
- The objective of minimizing the worst-case loss of a DG model at any distance in the representation space can be combined with losses of other DG methods to yield models that generalize better on unseen domains.

## Key results

- High worst-case loss even close to the source domains highlights the poor generalizability of current DG models.
- Worst-case loss in the representation space is not an overestimation of the worst-case loss in the input space.
  - Models trained with WM & G2DM on R-MNIST.



- Effectiveness of using different loss functions (cross entropy, hinge and misclassification) for computing the worst-case loss.
  - Models trained with WM on R-MNIST dataset and are evaluated using WC-DG.



## References

- Albuquerque et. al (2019), Generalizing to unseen domains via distribution matching.
- Long et. al (2018), Conditional adversarial domain adaptation.
- Krueger et. al (2021), Out-of-distribution generalization via risk extrapolation (rex).
- Sinha et. al (2017) Certifying some distributional robustness with principled adversarial training.
- Volpi et al (2018) Generalizing to unseen domains via adversarial data augmentation.